

Blockwise Repeated Burst Error Correcting Linear Codes

B.K. Dass

Department of Mathematics

University of Delhi

Delhi - 110 007, India

dassbk@rediffmail.com

Surbhi Madan *

Department of Mathematics

Shivaji College (University of Delhi)

New Delhi - 110 027, India

surbhimadan@gmail.com

Abstract

This paper presents a lower and an upper bound on the number of parity check digits required for a linear code that corrects a single sub-block containing errors which are in the form of 2-repeated bursts of length b or less. An illustration of such kind of codes has been provided. Further, the codes that correct m -repeated bursts of length b or less have also been studied.

Keywords: Error locating codes, error correction, burst errors, repeated burst errors

AMS Subject Classification: : 94B20, 94B65, 94B25.

*Corresponding Author

I Introduction

Error detecting codes and Error correcting codes have been the traditional areas of study in the field of coding techniques on error control in digital data transmission. Wolf and Elspas [12] introduced a coding technique, *error-locating codes* (EL Codes), lying midway between error detection and error correction. In an error locating code, each block of received digits is regarded as being subdivided into mutually exclusive sub-blocks, and codes have been devised that permit the detection of errors occurring within a single sub-block, the sub-block containing errors being identified. In ordinary decision feedback systems using error detection the receiver tests each block of received digits for the presence of errors. If errors are detected, the receiver requests the retransmission of the corrupted block of digits alone and this process is repeated for each incoming block. One drawback of the conventional system is that long block lengths (which are desirable for increased coding efficiency) can result in a low data rate when the reception of large amount of data is called for. However, the use of EL codes can soften this conflict between short and long block lengths by providing an additional design parameter. The overall constraint block length can be long to provide efficient coding while the length of the sub-blocks can be relatively short in order to keep the data rate up.

Codes developed at the early stages were meant mainly to detect and correct random errors. However, it was observed later that in many channels the likelihood of the occurrence of errors is more in adjacent positions rather than their occurrence in a random manner. In this spirit, Abramson[1] developed codes correcting single and double adjacent errors. The concept of clustered errors, commonly called burst errors, was generalized further in the work due to Fire [7]. A burst, also known as an open loop burst, of length b may be defined as follows:

Definition 1. A burst of length b is a vector whose all non-zero components are among some b consecutive components, the first and the last of which is non-zero.

It was observed that in very busy communication channels, errors repeat themselves. Similar is a situation when errors occur in the form of a burst. The development of codes for such kind of repeated burst errors is useful for

improving upon the efficiency of some communication channels. Not only do repeated bursts emerge as a natural generalization of bursts, but considering a recent study by Srinivas, Jain, Saurav and Sikdar [11], where the changes in the neuronal network properties during epileptiform activity *in vitro* in planar two-dimensional neuronal networks cultured on a multielectrode array using the *in vitro* model of stroke-induced epilepsy have been explored, we observe that the study of these codes is significant.

The study of codes that detect repeated open-loop bursts was initiated by Berardi, Dass and Verma [2] and for correction of such errors by Dass and Verma [6]. An m -repeated burst (open-loop) of length b is defined as follows:

Definition 2. An m -repeated burst of length b is a vector of length n whose only non-zero components are confined to m distinct sets of b consecutive components, the first and the last component of each set being non-zero.

For example, (001032000020310000313200) is a 3-repeated burst of length 4 over $GF(4)$.

In particular, a 2-repeated burst (open-loop) of length b is defined as:

Definition 3. A 2-repeated burst of length b is a vector of length n whose only non-zero components are confined to two distinct sets of b consecutive components, the first and the last component of each set being non-zero.

Wolf and Elspas [12] obtained results in the form of bounds over the number of parity-check digits required for binary codes capable of detecting and locating a single sub-block containing random errors. A study of such error locating codes in which errors occur in the form of bursts was made by Dass [3]. Further, these results were extended to the codes correcting burst errors occurring within a sub-block (refer Dass and Tyagi [5]). In our earlier paper [4] the authors obtained bounds over the number of parity-check digits required for codes detecting 2-repeated and m -repeated bursts of length b or less occurring within a single sub-block, the sub-block containing errors being identified. In this paper we extend our study to the correction of repeated bursts occurring within a sub-block. The development of codes correcting repeated burst errors within a sub-block improves the efficiency of the communication channel as it reduces the number of parity

check digits required. The results that follow have been described in terms of the following parameters: the block of n digits, consisting of r check digits, and $k = n - r$ information digits, is subdivided into s mutually exclusive sub-blocks, each sub-block containing $t = n/s$ digits.

II Bounds for codes correcting 2-repeated bursts

In this section, we obtain bounds on the number of parity check digits of a code capable of correcting 2-repeated bursts of length b or less occurring within a single sub-block.

We note that an (n, k) linear EL code over $GF(q)$ capable of detecting and locating a single sub-block containing 2-repeated burst of length b or less must satisfy the following two conditions:

- (i) The syndrome resulting from the occurrence of any 2-repeated burst of length b or less within any one sub-block must be non-zero.
- (ii) The syndrome resulting from the occurrence of any 2-repeated burst of length b or less within a single sub-block must be distinct from the syndrome resulting likewise from any 2-repeated burst of length b or less within *any other* sub-block.

Further, an (n, k) linear code over $GF(q)$ capable of correcting an error requires the syndromes of any two vectors to be distinct irrespective of whether they belong to the same sub-block or different sub-blocks. So, in order to correct 2-repeated bursts of length b or less lying within a sub-block the following conditions need to be satisfied:

- (iii) The syndrome resulting from the occurrence of any 2-repeated burst of length b or less within a single sub-block must be distinct from the syndrome resulting from any other 2-repeated burst of length b or less within the same sub-block.
- (iv) The syndrome resulting from the occurrence of any 2-repeated burst of length b or less within a single sub-block must be distinct from the syndrome resulting likewise from any 2-repeated burst of length b or less within *any other* sub-block.

Remark 1. We observe that condition (ii) is the same as condition (iv). Also, for computational purposes condition (i) is taken care of by condition (iii). From this we infer that correction of errors requires more strict conditions than location of

errors. So we need to consider conditions (iii) and (iv) or equivalently conditions (ii) and (iii) for correction of the said type of errors.

We first obtain a lower bound over the number of parity check digits required for such a code.

Theorem 1. *The number of check digits r required for an (n, k) linear code over $GF(q)$, subdivided into s sub-blocks of length t each, that corrects 2-repeated bursts of length b or less lying within a single corrupted sub-block is atleast*

$$\log_q \left\{ 1 + s \left[q^{2b-2} \left\{ q + (q-1)^2 \binom{t-2b+2}{2} + (q-1) \binom{t-2b+1}{1} \right\} - 1 \right] \right\}. \quad (1)$$

Proof. Let V be an (n, k) linear code over $GF(q)$ that corrects 2-repeated burst of length b or less within a single corrupted sub-block. The maximum number of distinct syndromes available using r check digits is q^r . The proof proceeds by first counting the number of syndromes that are required to be distinct by the two conditions and then setting this number less than or equal to q^r .

Since the code is capable of correcting all errors which are 2-repeated bursts of length b or less within any single sub-block, any syndrome produced by a 2-repeated burst of length b or less in a given sub-block must be distinct from any such syndrome likewise resulting from another 2-repeated burst of length b or less in the same sub-block (refer to condition (iii)). Moreover, syndromes produced by 2-repeated bursts of length b or less in different sub-blocks must also be distinct by condition (iv).

Thus, the syndromes of vectors which are 2-repeated bursts, whether in the same sub-block or in different sub-blocks, must be distinct.

Since there are

$$q^{2b-2} \left\{ q + (q-1)^2 \binom{t-2b+2}{2} + (q-1) \binom{t-2b+1}{1} \right\} - 1$$

2-repeated bursts of length b or less within one sub-block of length t , excluding the vector of all zeros (refer Dass and Verma (2008)) and there are s sub-blocks

in all, we must have at least

$$1 + s \left[q^{2b-2} \left\{ q + (q-1)^2 \binom{t-2b+2}{2} + (q-1) \binom{t-2b+1}{1} \right\} - 1 \right]$$

distinct syndromes, including the all zeros syndrome.

Therefore, we must have

$$q^r \geq 1 + s \left[q^{2b-2} \left\{ q + (q-1)^2 \binom{t-2b+2}{2} + (q-1) \binom{t-2b+1}{1} \right\} - 1 \right]$$

i.e.

$$r \geq \log_q \left\{ 1 + s \left[q^{2b-2} \left\{ q + (q-1)^2 \binom{t-2b+2}{2} + (q-1) \binom{t-2b+1}{1} \right\} - 1 \right] \right\}.$$

□

Remark 2. By taking $s = 1$ the bound obtained in (1) reduces to

$$\log_q \left(q^{2b-2} \left[q + (q-1)^2 \binom{t-2b+2}{2} + (q-1) \binom{t-2b+1}{1} \right] \right)$$

which coincides with the result for correction of 2-repeated bursts obtained by Dass and Verma(2008).

In the following result, we derive another bound on the number of check digits required for the existence of such a code. The proof is based on the technique used to establish Varshamov-Gilbert-Sacks bound by constructing a parity check matrix for such a code (refer Sacks (1958) also Theorem 4.7, Peterson and Weldon (1972)). This technique not only ensures the existence of such a code but also gives a method for the construction of the code.

Theorem 2. *An (n, k) linear code over $GF(q)$ capable of correcting 2-repeated burst of length b or less occurring within a single sub-block of length t ($4b < t$) can always be constructed using r check digits, where r is the smallest integer*

satisfying the inequality

$$q^r > q^{2(b-1)} \left\{ q^{2(b-1)} \left\{ (q-1)^3 \binom{t-4b+3}{3} + (q-1)^2 \binom{t-4b+2}{2} + q(q-1) \binom{t-4b+1}{1} + q^2 \right\} \right. \\ \left. + \left\{ (s-1) \left[(t-2b+1)(q-1) + 1 \right] \times \right. \right. \\ \left. \left. \left[q^{2(b-1)} \left\{ q + (q-1)^2 \binom{t-2b+2}{2} + (q-1) \binom{t-2b+1}{1} \right\} - 1 \right] \right\} \right\}. \quad (2)$$

Proof. We shall prove the result by constructing an appropriate $(n-k) \times n$ parity check matrix H for the desired code. Suppose that the columns of the first $s-1$ sub-blocks of H and the first $j-1$ columns h_1, h_2, \dots, h_{j-1} of the s^{th} sub-block have been appropriately added. We now lay down conditions to add the j^{th} column h_j to the s^{th} sub-block as follows:

Since the code is to correct 2-repeated bursts of length b or less within a single sub-block, therefore, by condition (iii), the syndrome of any 2-repeated burst in any sub-block must be different from the syndrome resulting from any other such burst within the same sub-block. Therefore the j^{th} column h_j can be added provided that h_j is not a linear combination of the immediately preceding $b-1$ or fewer columns $h_{j-b+1}, \dots, h_{j-1}$ of the s^{th} sub-block together with any three distinct sets of b or fewer consecutive columns each from amongst the first $j-b$ columns h_1, h_2, \dots, h_{j-b} . In other words,

$$h_j \neq (\alpha_1 h_{j-b+1} + \alpha_2 h_{j-b+2} + \dots + \alpha_{b-1} h_{j-1}) + \sum_{l=1}^3 (\beta_{l_1} h_{l_1} + \beta_{l_2} h_{l_2} + \dots + \beta_{l_b} h_{l_b}), \quad (3)$$

where $\alpha_i, \beta_{l_i} \in GF(q)$ and $l_b \leq j-b$.

The number of ways in which the coefficients α_i can be selected is clearly q^{b-1} . To enumerate the coefficients β_i is equivalent to enumerate the number of 3-repeated bursts of length b or less in a vector of length $j-b$ which is (refer Dass and Verma(2008))

$$q^{3(b-1)} \left\{ (q-1)^3 \binom{j-4b+3}{3} + (q-1)^2 \binom{j-4b+2}{2} + q(q-1) \binom{j-4b+1}{1} + q^2 \right\}.$$

Therefore, the total number of possible choices for α_i and β_i on the R.H.S of (3) is

$$q^{4(b-1)} \left\{ (q-1)^3 \binom{j-4b+3}{3} + (q-1)^2 \binom{j-4b+2}{2} + q(q-1) \binom{j-4b+1}{1} + q^2 \right\}. \quad (4)$$

Further, by condition (iv), h_j can be added to the s^{th} sub-block provided h_j is not a linear combination of the immediately preceding $b - 1$ or fewer columns together with one set of b or fewer columns from amongst the first $j - b$ columns together with linear combination of any two sets of b or less consecutive columns within *any other* sub-block. i.e.

$$\begin{aligned} h_j \neq & (\alpha_1 h_{j-b+1} + \alpha_2 h_{j-b+2} + \dots + \alpha_{b-1} h_{j-1}) + \\ & (\beta_1 h_i + \beta_2 h_{i+1} + \dots + \beta_b h_{i+b-1}) + \\ & (\gamma_1 h_{i_1} + \gamma_2 h_{i_1+1} + \dots + \gamma_b h_{i_1+b-1}) + \\ & (\delta_1 h_{i_2} + \delta_2 h_{i_2+1} + \dots + \delta_b h_{i_2+b-1}) \end{aligned} \quad (5)$$

where $\alpha_p, \beta_p, \gamma_p, \delta_p \in GF(q), i + b - 1 \leq j - b$ and not all γ_p and δ_p are zero. (The last two terms in the above sum correspond to any two sets of b or less consecutive columns within any one of the other sub-block.)

The number of ways in which the coefficients α_p can be selected is clearly q^{b-1} . To enumerate the coefficients β_p is equivalent to enumerate the number of bursts of length b or less in a vector of length $j - b$ which is $q^{b-1}[(j - 2b + 1)(q - 1) + 1]$ (refer Fire [7]). Therefore, the total number of possible choices for α_p and β_p on the R.H.S of (5) is

$$q^{2(b-1)} [(j - 2b + 1)(q - 1) + 1]. \quad (6)$$

Also, the number of linear combinations corresponding to the last two terms on the R.H.S. of (5) is the same as the number of 2-repeated bursts of length b or less within a sub-block of length t , excluding the vector of all zeros; which is (refer Dass and Verma (2008))

$$q^{2b-2} \left\{ q + (q-1)^2 \binom{t-2b+2}{2} + (q-1) \binom{t-2b+1}{1} \right\} - 1.$$

Since there are $s - 1$ previously chosen sub-blocks, the number of such linear combinations becomes

$$(s - 1) \left[q^{2b-2} \left\{ q + (q - 1)^2 \binom{t - 2b + 2}{2} + (q - 1) \binom{t - 2b + 1}{1} \right\} - 1 \right]. \quad (7)$$

Thus, the number of linear combinations to which h_j can not be equal to is the product computed in expr. (6) and expr. (7). i.e.

$$\text{expr.}(6) \times \text{expr.}(7). \quad (8)$$

Thus, the total number of linear combinations that h_j can not be equal to is the sum of linear combinations in (4) and (8).

At worst, all these combinations might yield a distinct sum. Therefore, h_j can be added to the s^{th} sub- block of H provided that

$$q^r > q^{2(b-1)} \left\{ q^{2(b-1)} \left\{ (q - 1)^3 \binom{j - 4b + 3}{3} + (q - 1)^2 \binom{j - 4b + 2}{2} + q(q - 1) \binom{j - 4b + 1}{1} + q^2 \right\} \right. \\ \left. + \left\{ (s - 1) [(j - 2b + 1)(q - 1) + 1] \times \right. \right. \\ \left. \left. \left[q^{2(b-1)} \left\{ q + (q - 1)^2 \binom{t - 2b + 2}{2} + (q - 1) \binom{t - 2b + 1}{1} \right\} - 1 \right] \right\} \right\}.$$

For completing the s^{th} sub-block of length t , replacing j by t gives the result as stated in (2). □

Remark 3. By taking $s = 1$ in (2) the bound reduces to

$$q^r > q^{4(b-1)} \left\{ (q - 1)^3 \binom{t - 4b + 3}{3} + (q - 1)^2 \binom{t - 4b + 2}{2} + q(q - 1) \binom{t - 4b + 1}{1} + q^2 \right\}$$

which coincides with the condition for existence of a code correcting 2-repeated bursts of length b or less(refer Dass and Verma(2008)).

We conclude this section with an example.

Example 1 Consider a (26, 10) binary code with a 16×26 parity-check matrix

Table 1
Error Patterns - Syndrome vectors

Sub-block 1

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
1	111111000000 000000000000	1111110000000000	44	011110100000 000000000000	0111101000000000
2	111011100000 000000000000	1110111000000000	45	011101010000 000000000000	0111010100000000
3	111001110000 000000000000	1110011100000000	46	011100101000 000000000000	0111001010000000
4	111000111000 000000000000	1110001110000000	47	011100010100 000000000000	0111000101000000
5	111000011100 000000000000	1110000111000000	48	011100001010 000000000000	0111000010100000
6	111000001110 000000000000	1110000011100000	49	011100000101 000000000000	0111000001010000
7	111000000111 000000000000	1110000001110000	50	011100000010 000000000000	0111000000101000
8	111000000011 000000000000	1110000000111000	51	011110000000 000000000000	0111100000000000
9	111101000000 000000000000	1111010000000000	52	011101100000 000000000000	0111011000000000
10	111101010000 000000000000	1111010100000000	53	011100110000 000000000000	0111001100000000
11	111100101000 000000000000	1111001010000000	54	011100011000 000000000000	0111000110000000
12	111100010100 000000000000	1111000101000000	55	011100001100 000000000000	0111000011000000
13	111100001010 000000000000	1111000010100000	56	011100000110 000000000000	0111000001100000
14	111100000101 000000000000	1111000001010000	57	011100000011 000000000000	0111000000110000
15	111100000010 000000000000	1111000000101000	58	011100000001 000000000000	0111000000011000
16	111100000001 000000000000	1111000000010100	59	011110000000 000000000000	0111100000000000
17	111110000000 000000000000	1111100000000000	60	011101000000 000000000000	0111010000000000
18	111101000000 000000000000	1111010000000000	61	011100100000 000000000000	0111001000000000
19	111100100000 000000000000	1111001000000000	62	011100010000 000000000000	0111000100000000
20	111100010000 000000000000	1111000100000000	63	011100001000 000000000000	0111000010000000
21	111100001000 000000000000	1111000010000000	64	011100000100 000000000000	0111000001000000
22	111100000100 000000000000	1111000001000000	65	011100000010 000000000000	0111000000100000
23	111100000010 000000000000	1111000000100000	66	011100000001 000000000000	0111000000010000
24	111100000001 000000000000	1111000000010000	67	011100000000 000000000000	0111000000001000
25	111100000000 000000000000	1111000000001100	68	011100000000 000000000000	0111000000000000
26	111100000000 000000000000	1111000000000000	69	001111110000 000000000000	0011111100000000
27	111101000000 000000000000	1111010000000000	70	001110111000 000000000000	0011101110000000
28	111100100000 000000000000	1111001000000000	71	001110011100 000000000000	0011100111000000
29	111100010000 000000000000	1111000100000000	72	001110001110 000000000000	0011100011100000
30	111100001000 000000000000	1111000010000000	73	001110000111 000000000000	0011100001110000
31	111100000100 000000000000	1111000001000000	74	001110000011 000000000000	0011100000111000
32	111100000010 000000000000	1111000000100000	75	001111010000 000000000000	0011110100000000
33	111100000001 000000000000	1111000000010000	76	001110101000 000000000000	0011101010000000
34	111100000000 000000000000	1111000000001000	77	001110010100 000000000000	0011100101000000
35	111100000000 000000000000	1111000000000100	78	001110001010 000000000000	0011100010100000
36	111100000000 000000000000	1111000000000000	79	001110000101 000000000000	0011100001010000
37	011111100000 000000000000	0111111000000000	80	001110000010 000000000000	0011100000101000
38	011101110000 000000000000	0111011100000000	81	001111100000 000000000000	0011111000000000
39	011100111000 000000000000	0111001110000000	82	001110110000 000000000000	0011101100000000
40	011100011100 000000000000	0111000111000000	83	001110011000 000000000000	0011100110000000
41	011100001110 000000000000	0111000011100000	84	001110001100 000000000000	0011100011000000
42	011100000111 000000000000	0111000001110000	85	001110000110 000000000000	0011100001100000
43	011100000011 000000000000	0111000000111000	86	001110000011 000000000000	0011100000110000

Sub-block 1

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
87	001110000011 000000000000	001110000011000	134	0000111100000 000000000000	0000111100000000
88	001111000000 000000000000	001111000000000	135	0000111010000 000000000000	0000111010000000
89	001110100000 000000000000	001110100000000	136	0000111001000 000000000000	0000111001000000
90	001110010000 000000000000	001110010000000	137	0000111000100 000000000000	0000111000100000
91	001110001000 000000000000	001110001000000	138	0000111000010 000000000000	0000111000010000
92	0011100001000 000000000000	001110000100000	139	0000111000001 000000000000	0000111000001000
93	0011100000100 000000000000	001110000010000	140	0000111000000 000000000000	0000111000000000
94	0011100000010 000000000000	001110000001000	141	0000011111100 000000000000	0000011111100000
95	0011100000001 000000000000	0011100000001000	142	0000011101110 000000000000	0000011101110000
96	0011100000000 000000000000	0011100000000000	143	0000011100111 000000000000	0000011100111000
97	0001111110000 000000000000	000111111000000	144	0000011110100 000000000000	0000011110100000
98	0001110111000 000000000000	000111011100000	145	0000011101010 000000000000	0000011101010000
99	0001110011100 000000000000	000111001110000	146	0000011100101 000000000000	0000011100101000
100	0001110001110 000000000000	000111000111000	147	0000011111000 000000000000	0000011111000000
101	0001110000111 000000000000	0001110000111000	148	0000011101100 000000000000	0000011101100000
102	0001111010000 000000000000	000111101000000	149	0000011100110 000000000000	0000011100110000
103	0001110101000 000000000000	000111010100000	150	0000011100011 000000000000	0000011100011000
104	0001110010100 000000000000	000111001010000	151	0000011110000 000000000000	0000011110000000
105	0001110001010 000000000000	000111000101000	152	0000011101000 000000000000	0000011101000000
106	0001110000101 000000000000	0001110000101000	153	0000011100100 000000000000	0000011100100000
107	0001111110000 000000000000	000111111000000	154	0000011100010 000000000000	0000011100010000
108	0001110110000 000000000000	000111011000000	155	0000011100001 000000000000	0000011100001000
109	0001110011000 000000000000	000111001100000	156	0000011100000 000000000000	0000011100000000
110	0001110001100 000000000000	000111000110000	157	0000001111110 000000000000	0000001111110000
111	0001110000110 000000000000	000111000011000	158	0000001110111 000000000000	0000001110111000
112	0001110000011 000000000000	0001110000011000	159	0000001111010 000000000000	0000001111010000
113	0001111000000 000000000000	000111100000000	160	0000001110101 000000000000	0000001110101000
114	0001110100000 000000000000	000111010000000	161	0000001111100 000000000000	0000001111100000
115	0001110010000 000000000000	000111001000000	162	0000001110110 000000000000	0000001110110000
116	0001110001000 000000000000	000111000100000	163	0000001110011 000000000000	0000001110011000
117	0001110000100 000000000000	000111000010000	164	0000001111000 000000000000	0000001111000000
118	0001110000010 000000000000	000111000001000	165	0000001110100 000000000000	0000001110100000
119	0001110000001 000000000000	0001110000001000	166	0000001110010 000000000000	0000001110010000
120	0001110000000 000000000000	000111000000000	167	0000001110001 000000000000	0000001110001000
121	0000111111000 000000000000	000011111100000	168	0000001110000 000000000000	0000001110000000
122	0000111011100 000000000000	000011101110000	169	0000000111111 000000000000	0000000111111000
123	0000111001110 000000000000	000011100111000	170	0000000111010 000000000000	0000000111010000
124	0000111000111 000000000000	0000111000111000	171	0000000111110 000000000000	0000000111110000
125	0000111101000 000000000000	000011110100000	172	0000000111011 000000000000	0000000111011000
126	0000111010100 000000000000	000011101010000	173	0000000111100 000000000000	0000000111100000
127	0000111001010 000000000000	000011100101000	174	0000000111010 000000000000	0000000111010000
128	0000111000101 000000000000	0000111000101000	175	0000000111001 000000000000	0000000111001000
129	0000111100000 000000000000	000011110000000	176	0000000111000 000000000000	0000000111000000
130	0000111011000 000000000000	000011101100000	177	0000000011111 000000000000	0000000011111000
131	0000111001100 000000000000	000011100110000	178	0000000011101 000000000000	0000000011101000
132	0000111000110 000000000000	000011100011000	179	0000000011110 000000000000	0000000011110000
133	0000111000011 000000000000	0000111000011000	180	0000000011100 000000000000	0000000011100000

Sub-block 1

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
181	000000001111 000000000000	000000001111000	228	010101010000 000000000000	010101010000000
182	000000001110 000000000000	000000001110000	229	010100101000 000000000000	010100101000000
183	000000000111 000000000000	000000000111000	230	010100010100 000000000000	010100010100000
184	101111000000 000000000000	101111000000000	231	010100001010 000000000000	010100001010000
185	101011100000 000000000000	101011100000000	232	010100000101 000000000000	010100000101000
186	101001110000 000000000000	101001110000000	233	010100000010 000000000000	010100000010100
187	101000111000 000000000000	101000111000000	234	010111000000 000000000000	010111000000000
188	101000011100 000000000000	101000011100000	235	010101100000 000000000000	010101100000000
189	101000001110 000000000000	101000001110000	236	010100110000 000000000000	010100110000000
190	101000000111 000000000000	101000000111000	237	010100011000 000000000000	010100011000000
191	101000000011 000000000000	101000000011100	238	010100001100 000000000000	010100001100000
192	101101000000 000000000000	101101000000000	239	010100000110 000000000000	010100000110000
193	101010100000 000000000000	101010100000000	240	010100000011 000000000000	010100000011000
194	101001010000 000000000000	101001010000000	241	010100000001 000000000000	010100000001100
195	101000101000 000000000000	101000101000000	242	010110000000 000000000000	010110000000000
196	101000010100 000000000000	101000010100000	243	010101000000 000000000000	010101000000000
197	101000001010 000000000000	101000001010000	244	010100100000 000000000000	010100100000000
198	101000000101 000000000000	101000000101000	245	010100010000 000000000000	010100010000000
199	101000000010 000000000000	101000000010100	246	010100001000 000000000000	010100001000000
200	101110000000 000000000000	101110000000000	247	010100000100 000000000000	010100000100000
201	101011000000 000000000000	101011000000000	248	010100000010 000000000000	010100000010000
202	101001100000 000000000000	101001100000000	249	010100000001 000000000000	010100000001000
203	101000110000 000000000000	101000110000000	250	010100000000 000000000000	010100000000000
204	101000011000 000000000000	101000011000000	251	001011110000 000000000000	001011110000000
205	101000000110 000000000000	101000000110000	252	001010111000 000000000000	001010111000000
206	101000000011 000000000000	101000000011100	253	001010011100 000000000000	001010011100000
207	101000000001 000000000000	101000000001100	254	001010001110 000000000000	001010001110000
208	101100000000 000000000000	101100000000000	255	001010000110 000000000000	001010000110000
209	101010000000 000000000000	101010000000000	256	001010000111 000000000000	001010000111000
210	101001000000 000000000000	101001000000000	257	001010000011 000000000000	001010000011100
211	101001000000 000000000000	101001000000000	258	001011010000 000000000000	001011010000000
212	101000100000 000000000000	101000100000000	259	001010101000 000000000000	001010101000000
213	101000010000 000000000000	101000010000000	260	001010010100 000000000000	001010010100000
214	101000001000 000000000000	101000001000000	261	001010001010 000000000000	001010001010000
215	101000000100 000000000000	101000000100000	262	001010000101 000000000000	001010000101000
216	101000000010 000000000000	101000000010000	263	001010000010 000000000000	001010000010100
217	101000000001 000000000000	101000000001000	264	001010000001 000000000000	001010000001100
218	101000000000 000000000000	101000000000000	265	001010110000 000000000000	001010110000000
219	101000000000 000000000000	101000000000000	266	001010011000 000000000000	001010011000000
220	010111100000 000000000000	010111100000000	267	001010001100 000000000000	001010001100000
221	010101110000 000000000000	010101110000000	268	001010000110 000000000000	001010000110000
222	010100111000 000000000000	010100111000000	269	001010000011 000000000000	001010000011000
223	010100011100 000000000000	010100011100000	270	001010000001 000000000000	001010000001100
224	010100001110 000000000000	010100001110000	271	001011000000 000000000000	001011000000000
225	010100000111 000000000000	010100000111000	272	001010100000 000000000000	001010100000000
226	010100000011 000000000000	010100000011100	273	001010010000 000000000000	001010010000000
227	010110100000 000000000000	010110100000000	274	001010001000 000000000000	001010001000000

Sub-block 1

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
275	0010100001000 0000000000000	0010100001000000	322	0000101000001 0000000000000	0000101000001000
276	0010100000100 0000000000000	0010100000100000	323	0000101000000 0000000000000	0000101000000000
277	0010100000010 0000000000000	0010100000010000	324	0000010111100 0000000000000	0000010111100000
278	0010100000001 0000000000000	0010100000001000	325	0000010101110 0000000000000	0000010101110000
279	0010100000000 0000000000000	0010100000000000	326	0000010100111 0000000000000	0000010100111000
280	0001011110000 0000000000000	0001011110000000	327	0000010110100 0000000000000	0000010110100000
281	0001010111000 0000000000000	0001010111000000	328	0000010101010 0000000000000	0000010101010000
282	0001010011100 0000000000000	0001010011100000	329	0000010100101 0000000000000	0000010100101000
283	0001010001110 0000000000000	0001010001110000	330	0000010111000 0000000000000	0000010111000000
284	0001010000111 0000000000000	0001010000111000	331	0000010101100 0000000000000	0000010101100000
285	0001011010000 0000000000000	0001011010000000	332	0000010100110 0000000000000	0000010100110000
286	0001010101000 0000000000000	0001010101000000	333	0000010100011 0000000000000	0000010100011000
287	0001010010100 0000000000000	0001010010100000	334	0000010110000 0000000000000	0000010110000000
288	0001010001010 0000000000000	0001010001010000	335	0000010101000 0000000000000	0000010101000000
289	0001010000101 0000000000000	0001010000101000	336	0000010100100 0000000000000	0000010100100000
290	0001011100000 0000000000000	0001011100000000	337	0000010100010 0000000000000	0000010100010000
291	0001010110000 0000000000000	0001010110000000	338	0000010100001 0000000000000	0000010100001000
292	0001010011000 0000000000000	0001010011000000	339	0000010100000 0000000000000	0000010100000000
293	0001010001100 0000000000000	0001010001100000	340	0000001011110 0000000000000	0000001011110000
294	0001010000110 0000000000000	0001010000110000	341	0000001010111 0000000000000	0000001010111000
295	0001010000011 0000000000000	0001010000011000	342	0000001011010 0000000000000	0000001011010000
296	0001011000000 0000000000000	0001011000000000	343	0000001010101 0000000000000	0000001010101000
297	0001010100000 0000000000000	0001010100000000	344	0000001011100 0000000000000	0000001011100000
298	0001010010000 0000000000000	0001010010000000	345	0000001010110 0000000000000	0000001010110000
299	0001010001000 0000000000000	0001010001000000	346	0000001010011 0000000000000	0000001010011000
300	0001010000100 0000000000000	0001010000100000	347	0000001011000 0000000000000	0000001011000000
301	0001010000010 0000000000000	0001010000010000	348	0000001010100 0000000000000	0000001010100000
302	0001010000001 0000000000000	0001010000001000	349	0000001010010 0000000000000	0000001010010000
303	0001010000000 0000000000000	0001010000000000	350	0000001010001 0000000000000	0000001010001000
304	0000101111000 0000000000000	0000101111000000	351	0000001010000 0000000000000	0000001010000000
305	0000101011100 0000000000000	0000101011100000	352	0000000101111 0000000000000	0000000101111000
306	0000101001110 0000000000000	0000101001110000	353	0000000101101 0000000000000	0000000101101000
307	0000101000111 0000000000000	0000101000111000	354	0000000101110 0000000000000	0000000101110000
308	0000101101000 0000000000000	0000101101000000	355	0000000101011 0000000000000	0000000101011000
309	0000101010100 0000000000000	0000101010100000	356	0000000101100 0000000000000	0000000101100000
310	0000101001010 0000000000000	0000101001010000	357	0000000101010 0000000000000	0000000101010000
311	0000101000101 0000000000000	0000101000101000	358	0000000101001 0000000000000	0000000101001000
312	0000101110000 0000000000000	0000101110000000	359	0000000101000 0000000000000	0000000101000000
313	0000101011000 0000000000000	0000101011000000	360	0000000010111 0000000000000	0000000010111000
314	0000101001100 0000000000000	0000101001100000	361	0000000010101 0000000000000	0000000010101000
315	0000101000110 0000000000000	0000101000110000	362	0000000010110 0000000000000	0000000010110000
316	0000101000011 0000000000000	0000101000011000	363	0000000010100 0000000000000	0000000010100000
317	0000101100000 0000000000000	0000101100000000	364	0000000001011 0000000000000	0000000001011000
318	0000101010000 0000000000000	0000101010000000	365	0000000001010 0000000000000	0000000001010000
319	0000101001000 0000000000000	0000101001000000	366	0000000000101 0000000000000	0000000000101000
320	0000101000100 0000000000000	0000101000100000	367	1101110000000 0000000000000	1101110000000000
321	0000101000010 0000000000000	0000101000010000	368	1100111000000 0000000000000	1100111000000000

Sub-block 1

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
369	110001110000 000000000000	1100011100000000	416	0110000000101 000000000000	0110000000101000
370	1100001110000 000000000000	1100001110000000	417	0110110000000 000000000000	0110110000000000
371	1100000111000 000000000000	1100000111000000	418	0110011000000 000000000000	0110011000000000
372	1100000011100 000000000000	1100000011100000	419	0110001100000 000000000000	0110001100000000
373	1100000001110 000000000000	1100000001110000	420	0110000110000 000000000000	0110000110000000
374	1100000000111 000000000000	1100000000111000	421	0110000011000 000000000000	0110000011000000
375	1101010000000 000000000000	1101010000000000	422	0110000001100 000000000000	0110000001100000
376	1100101000000 000000000000	1100101000000000	423	0110000000110 000000000000	0110000000110000
377	1100010100000 000000000000	1100010100000000	424	0110000000011 000000000000	0110000000011000
378	1100001010000 000000000000	1100001010000000	425	0110100000000 000000000000	0110100000000000
379	1100000101000 000000000000	1100000101000000	426	0110010000000 000000000000	0110010000000000
380	1100000010100 000000000000	1100000010100000	427	0110001000000 000000000000	0110001000000000
381	1100000001010 000000000000	1100000001010000	428	0110000100000 000000000000	0110000100000000
382	1100000000101 000000000000	1100000000101000	429	0110000010000 000000000000	0110000010000000
383	1101100000000 000000000000	1101100000000000	430	0110000001000 000000000000	0110000001000000
384	1100110000000 000000000000	1100110000000000	431	0110000000100 000000000000	0110000000100000
385	1100011000000 000000000000	1100011000000000	432	0110000000010 000000000000	0110000000010000
386	1100001100000 000000000000	1100001100000000	433	0110000000001 000000000000	0110000000001000
387	1100000110000 000000000000	1100000110000000	434	0110000000000 000000000000	0110000000000000
388	1100000011000 000000000000	1100000011000000	435	0011011100000 000000000000	0011011100000000
389	1100000001100 000000000000	1100000001100000	436	0011001110000 000000000000	0011001110000000
390	1100000000110 000000000000	1100000000110000	437	0011000111000 000000000000	0011000111000000
391	1100000000011 000000000000	1100000000011000	438	0011000011100 000000000000	0011000011100000
392	1101000000000 000000000000	1101000000000000	439	0011000001110 000000000000	0011000001110000
393	1100100000000 000000000000	1100100000000000	440	0011000000111 000000000000	0011000000111000
394	1100010000000 000000000000	1100010000000000	441	0011010100000 000000000000	0011010100000000
395	1100001000000 000000000000	1100001000000000	442	0011001010000 000000000000	0011001010000000
396	1100000100000 000000000000	1100000100000000	443	0011000101000 000000000000	0011000101000000
397	1100000010000 000000000000	1100000010000000	444	0011000010100 000000000000	0011000010100000
398	1100000001000 000000000000	1100000001000000	445	0011000001010 000000000000	0011000001010000
399	1100000000100 000000000000	1100000000100000	446	0011000000101 000000000000	0011000000101000
400	1100000000010 000000000000	1100000000010000	447	0011011000000 000000000000	0011011000000000
401	1100000000001 000000000000	1100000000001000	448	0011001100000 000000000000	0011001100000000
402	1100000000000 000000000000	1100000000000000	449	0011000110000 000000000000	0011000110000000
403	0110111000000 000000000000	0110111000000000	450	0011000011000 000000000000	0011000011000000
404	0110011100000 000000000000	0110011100000000	451	0011000001100 000000000000	0011000001100000
405	0110001110000 000000000000	0110001110000000	452	0011000000110 000000000000	0011000000110000
406	0110000111000 000000000000	0110000111000000	453	0011000000011 000000000000	0011000000011000
407	0110000011100 000000000000	0110000011100000	454	0011010000000 000000000000	0011010000000000
408	0110000001110 000000000000	0110000001110000	455	0011001000000 000000000000	0011001000000000
409	0110000000111 000000000000	0110000000111000	456	0011000100000 000000000000	0011000100000000
410	0110101000000 000000000000	0110101000000000	457	0011000010000 000000000000	0011000010000000
411	0110010100000 000000000000	0110010100000000	458	0011000001000 000000000000	0011000001000000
412	0110001010000 000000000000	0110001010000000	459	0011000000100 000000000000	0011000000100000
413	0110000101000 000000000000	0110000101000000	460	0011000000010 000000000000	0011000000010000
414	0110000010100 000000000000	0110000010100000	461	0011000000001 000000000000	0011000000001000
415	0110000001010 000000000000	0110000001010000	462	0011000000000 000000000000	0011000000000000

Sub-block 1

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
463	0001101110000 0000000000000	0001101110000000	510	0000011010100 0000000000000	0000011010100000
464	0001100111000 0000000000000	0001100111000000	511	0000011001010 0000000000000	0000011001010000
465	0001100011100 0000000000000	0001100011100000	512	0000011000101 0000000000000	0000011000101000
466	0001100001110 0000000000000	0001100001110000	513	0000011011000 0000000000000	0000011011000000
467	0001100000111 0000000000000	0001100000111000	514	0000011001100 0000000000000	0000011001100000
468	0001101010000 0000000000000	0001101010000000	515	0000011000110 0000000000000	0000011000110000
469	0001100101000 0000000000000	0001100101000000	516	0000011000011 0000000000000	0000011000011000
470	0001100010100 0000000000000	0001100010100000	517	0000011010000 0000000000000	0000011010000000
471	0001100001010 0000000000000	0001100001010000	518	0000011001000 0000000000000	0000011001000000
472	0001100000101 0000000000000	0001100000101000	519	0000011000100 0000000000000	0000011000100000
473	0001101100000 0000000000000	0001101100000000	520	0000011000010 0000000000000	0000011000010000
474	0001100110000 0000000000000	0001100110000000	521	0000011000001 0000000000000	0000011000001000
475	0001100011000 0000000000000	0001100011000000	522	0000011000000 0000000000000	0000011000000000
476	0001100001100 0000000000000	0001100001100000	523	0000001101110 0000000000000	0000001101110000
477	0001100000110 0000000000000	0001100000110000	524	0000001100111 0000000000000	0000001100111000
478	0001100000011 0000000000000	0001100000011000	525	0000001101010 0000000000000	0000001101010000
479	0001101000000 0000000000000	0001101000000000	526	0000001100101 0000000000000	0000001100101000
480	0001100100000 0000000000000	0001100100000000	527	0000001101100 0000000000000	0000001101100000
481	0001100010000 0000000000000	0001100010000000	528	0000001100110 0000000000000	0000001100110000
482	0001100001000 0000000000000	0001100001000000	529	0000001100011 0000000000000	0000001100011000
483	0001100000100 0000000000000	0001100000100000	530	0000001101000 0000000000000	0000001101000000
484	0001100000010 0000000000000	0001100000010000	531	0000001100100 0000000000000	0000001100100000
485	0001100000001 0000000000000	0001100000001000	532	0000001100010 0000000000000	0000001100010000
486	0001100000000 0000000000000	0001100000000000	533	0000001100001 0000000000000	0000001100001000
487	0000110111000 0000000000000	0000110111000000	534	0000001100000 0000000000000	0000001100000000
488	0000110011100 0000000000000	0000110011100000	535	0000000110111 0000000000000	0000000110111000
489	0000110001110 0000000000000	0000110001110000	536	0000000110101 0000000000000	0000000110101000
490	0000110000111 0000000000000	0000110000111000	537	0000000110110 0000000000000	0000000110110000
491	0000110101000 0000000000000	0000110101000000	538	0000000110011 0000000000000	0000000110011000
492	0000110010100 0000000000000	0000110010100000	539	0000000110100 0000000000000	0000000110100000
493	0000110001010 0000000000000	0000110001010000	540	0000000110010 0000000000000	0000000110010000
494	0000110000101 0000000000000	0000110000101000	541	0000000110001 0000000000000	0000000110001000
495	0000110110000 0000000000000	0000110110000000	542	0000000110000 0000000000000	0000000110000000
496	0000110011000 0000000000000	0000110011000000	543	0000000011011 0000000000000	0000000011011000
497	0000110001100 0000000000000	0000110001100000	544	0000000011001 0000000000000	0000000011001000
498	0000110000110 0000000000000	0000110000110000	545	0000000011010 0000000000000	0000000011010000
499	0000110000011 0000000000000	0000110000011000	546	0000000011000 0000000000000	0000000011000000
500	0000110100000 0000000000000	0000110100000000	547	0000000001101 0000000000000	0000000001101000
501	0000110010000 0000000000000	0000110010000000	548	0000000001100 0000000000000	0000000001100000
502	0000110001000 0000000000000	0000110001000000	549	0000000000110 0000000000000	0000000000110000
503	0000110000100 0000000000000	0000110000100000	550	0000000000011 0000000000000	0000000000011000
504	0000110000010 0000000000000	0000110000010000	551	1001110000000 0000000000000	1001110000000000
505	0000110000001 0000000000000	0000110000001000	552	1000111000000 0000000000000	1000111000000000
506	0000110000000 0000000000000	0000110000000000	553	1000011100000 0000000000000	1000011100000000
507	0000011011100 0000000000000	0000011011100000	554	1000001110000 0000000000000	1000001110000000
508	0000011001110 0000000000000	0000011001110000	555	1000000111000 0000000000000	1000000111000000
509	0000011000111 0000000000000	0000011000111000	556	1000000011100 0000000000000	1000000011100000

Sub-block 1

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
557	100000001110 000000000000	100000001110000	604	0100000110000 000000000000	0100000110000000
558	100000000111 000000000000	100000000111000	605	0100000011000 000000000000	0100000011000000
559	100101000000 000000000000	100101000000000	606	0100000001100 000000000000	0100000001100000
560	100010100000 000000000000	100010100000000	607	0100000000110 000000000000	0100000000110000
561	100001010000 000000000000	100001010000000	608	0100000000011 000000000000	0100000000011000
562	100000101000 000000000000	100000101000000	609	0100100000000 000000000000	0100100000000000
563	100000010100 000000000000	100000010100000	610	0100010000000 000000000000	0100010000000000
564	100000001010 000000000000	100000001010000	611	0100001000000 000000000000	0100001000000000
565	100000000101 000000000000	100000000101000	612	0100000100000 000000000000	0100000100000000
566	100000000010 000000000000	100000000010100	613	0100000010000 000000000000	0100000010000000
567	100110000000 000000000000	100110000000000	614	0100000001000 000000000000	0100000001000000
568	100011000000 000000000000	100011000000000	615	0100000000100 000000000000	0100000000100000
569	100001100000 000000000000	100001100000000	616	0100000000010 000000000000	0100000000010000
570	100000110000 000000000000	100000110000000	617	0100000000001 000000000000	0100000000001000
571	100000011000 000000000000	100000011000000	618	0100000000000 000000000000	0100000000000000
572	100000001100 000000000000	100000001100000	619	0010011100000 000000000000	0010011100000000
573	100000000110 000000000000	100000000110000	620	0010001110000 000000000000	0010001110000000
574	100000000011 000000000000	100000000011000	621	0010000111000 000000000000	0010000111000000
575	100000000001 000000000000	100000000001000	622	0010000011100 000000000000	0010000011100000
576	100100000000 000000000000	100100000000000	623	0010000001110 000000000000	0010000001110000
577	100010000000 000000000000	100010000000000	624	0010000000111 000000000000	0010000000111000
578	100001000000 000000000000	100001000000000	625	0010010100000 000000000000	0010010100000000
579	100000100000 000000000000	100000100000000	626	0010001010000 000000000000	0010001010000000
580	100000010000 000000000000	100000010000000	627	0010000101000 000000000000	0010000101000000
581	100000001000 000000000000	100000001000000	628	0010000010100 000000000000	0010000010100000
582	100000000100 000000000000	100000000100000	629	0010000001010 000000000000	0010000001010000
583	100000000010 000000000000	100000000010000	630	0010000000101 000000000000	0010000000101000
584	100000000001 000000000000	100000000001000	631	0010011000000 000000000000	0010011000000000
585	100000000000 000000000000	100000000000000	632	0010001100000 000000000000	0010001100000000
586	100000000000 000000000000	100000000000000	633	0010000110000 000000000000	0010000110000000
587	010011100000 000000000000	010011100000000	634	0010000011000 000000000000	0010000011000000
588	010001110000 000000000000	010001110000000	635	0010000001100 000000000000	0010000001100000
589	010000111000 000000000000	010000111000000	636	0010000000110 000000000000	0010000000110000
590	010000011100 000000000000	010000011100000	637	0010000000011 000000000000	0010000000011000
591	010000001110 000000000000	010000001110000	638	0010010000000 000000000000	0010010000000000
592	010000000111 000000000000	010000000111000	639	0010001000000 000000000000	0010001000000000
593	010000000011 000000000000	010000000011000	640	0010000100000 000000000000	0010000100000000
594	010010100000 000000000000	010010100000000	641	0010000010000 000000000000	0010000010000000
595	010001010000 000000000000	010001010000000	642	0010000001000 000000000000	0010000001000000
596	010000101000 000000000000	010000101000000	643	0010000000100 000000000000	0010000000100000
597	010000010100 000000000000	010000010100000	644	0010000000010 000000000000	0010000000010000
598	010000001010 000000000000	010000001010000	645	0010000000001 000000000000	0010000000001000
599	010000000101 000000000000	010000000101000	646	0010000000000 000000000000	0010000000000000
600	010000000010 000000000000	010000000010000	647	0001001110000 000000000000	0001001110000000
601	010011000000 000000000000	010011000000000	648	0001000111000 000000000000	0001000111000000
602	010001100000 000000000000	010001100000000	649	0001000011100 000000000000	0001000011100000
603	010000110000 000000000000	010000110000000	650	0001000001110 000000000000	0001000001110000

Sub-block 1

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
651	0001000000111 0000000000000	0001000000111000	694	0000010010100 0000000000000	0000010010100000
652	0001001010000 0000000000000	0001001010000000	695	0000010001010 0000000000000	0000010001010000
653	0001000101000 0000000000000	0001000101000000	696	0000010000101 0000000000000	0000010000101000
654	0001000010100 0000000000000	0001000010100000	697	0000010011000 0000000000000	0000010011000000
655	0001000001010 0000000000000	0001000001010000	698	0000010001100 0000000000000	0000010001100000
656	0001000000101 0000000000000	0001000000101000	699	0000010000110 0000000000000	0000010000110000
657	0001001100000 0000000000000	0001001100000000	700	0000010000011 0000000000000	0000010000011000
658	0001000110000 0000000000000	0001000110000000	701	0000010010000 0000000000000	0000010010000000
659	0001000011000 0000000000000	0001000011000000	702	0000010001000 0000000000000	0000010001000000
660	0001000001100 0000000000000	0001000001100000	703	0000010000100 0000000000000	0000010000100000
661	0001000000110 0000000000000	0001000000110000	704	0000010000010 0000000000000	0000010000010000
662	0001000000011 0000000000000	0001000000011000	705	0000010000001 0000000000000	0000010000001000
663	0001001000000 0000000000000	0001001000000000	706	0000010000000 0000000000000	0000010000000000
664	0001000100000 0000000000000	0001000100000000	707	0000001001110 0000000000000	0000001001110000
665	0001000010000 0000000000000	0001000010000000	708	0000001000111 0000000000000	0000001000111000
666	0001000001000 0000000000000	0001000001000000	709	0000001001010 0000000000000	0000001001010000
667	0001000000100 0000000000000	0001000000100000	710	0000001000101 0000000000000	0000001000101000
668	0001000000010 0000000000000	0001000000010000	711	0000001001100 0000000000000	0000001001100000
669	0001000000001 0000000000000	0001000000001000	712	0000001000110 0000000000000	0000001000110000
670	0001000000000 0000000000000	0001000000000000	713	0000001000011 0000000000000	0000001000011000
671	0000100111000 0000000000000	0000100111000000	714	0000001001000 0000000000000	0000001001000000
672	0000100011100 0000000000000	0000100011100000	715	0000001000100 0000000000000	0000001000100000
673	0000100001110 0000000000000	0000100001110000	716	0000001000010 0000000000000	0000001000010000
674	0000100000111 0000000000000	0000100000111000	717	0000001000001 0000000000000	0000001000001000
675	0000100101000 0000000000000	0000100101000000	718	0000001000000 0000000000000	0000001000000000
676	0000100010100 0000000000000	0000100010100000	719	0000000100111 0000000000000	0000000100111000
677	0000100001010 0000000000000	0000100001010000	720	0000000100101 0000000000000	0000000100101000
678	0000100000101 0000000000000	0000100000101000	721	0000000100110 0000000000000	0000000100110000
679	0000100110000 0000000000000	0000100110000000	722	0000000100011 0000000000000	0000000100011000
680	0000100011000 0000000000000	0000100011000000	723	0000000100100 0000000000000	0000000100100000
681	0000100001100 0000000000000	0000100001100000	724	0000000100010 0000000000000	0000000100010000
682	0000100000110 0000000000000	0000100000110000	725	0000000100001 0000000000000	0000000100001000
683	0000100000011 0000000000000	0000100000011000	726	0000000100000 0000000000000	0000000100000000
684	0000100100000 0000000000000	0000100100000000	727	0000000010011 0000000000000	0000000010011000
685	0000100010000 0000000000000	0000100010000000	728	0000000010001 0000000000000	0000000010001000
686	0000100001000 0000000000000	0000100001000000	729	0000000010010 0000000000000	0000000010010000
687	0000100000100 0000000000000	0000100000100000	730	0000000010000 0000000000000	0000000010000000
688	0000100000010 0000000000000	0000100000010000	731	0000000001001 0000000000000	0000000001001000
689	0000100000001 0000000000000	0000100000001000	732	0000000000100 0000000000000	0000000000100000
690	0000100000000 0000000000000	0000100000000000	733	0000000000010 0000000000000	0000000000010000
691	0000010011100 0000000000000	0000010011100000	734	0000000000010 0000000000000	0000000000010000
692	0000010001110 0000000000000	0000010001110000	735	0000000000001 0000000000000	0000000000001000
693	0000010000111 0000000000000	0000010000111000			

Sub-block 2

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
736	000000000000 111111000000	0000111111111101	779	000000000000 011110100000	000010010000100
737	000000000000 110111000000	0000111111101010	780	000000000000 011101010000	0000111111100101
738	000000000000 110011100000	0000111111101110	781	000000000000 011100101000	0000100101110100
739	000000000000 110001110000	0000111101101010	782	000000000000 011100010100	0001011010011100
740	000000000000 110000111000	0001110110110000	783	000000000000 011100001010	0000000000110111
741	000000000000 110000011100	0001001000100000	784	000000000000 0111000001010	0011001010011010
742	000000000000 110000001110	0011101111001010	785	000000000000 0111000000101	0001100000001101
743	000000000000 110000000111	0011101011001011	786	000000000000 011111000000	0000111111111001
744	000000000000 111101000000	0000101101101101	787	000000000000 011101100000	0000100100110110
745	000000000000 111010100000	0000011011001000	788	000000000000 011100110000	0000010010011000
746	000000000000 111001010000	0000110110101001	789	000000000000 011100011000	0000111110100111
747	000000000000 111000101000	0000101100111000	790	000000000000 011100001100	0001101101110000
748	000000000000 111000010100	0001010011010000	791	000000000000 0111000001100	0001100100001100
749	000000000000 111000001010	0000001001111011	792	000000000000 0111000000110	0010100111011101
750	000000000000 1110000001010	0011000011010110	793	000000000000 0111000000011	0011001110011011
751	000000000000 1110000000101	0001101001000001	794	000000000000 011110000000	0000011011011011
752	000000000000 111110000000	0000011011011111	795	000000000000 011101000000	0000101101101001
753	000000000000 111011000000	0000110110110101	796	000000000000 011100100000	0000000000010100
754	000000000000 111001100000	0000101101111010	797	000000000000 011100010000	0000011011000111
755	000000000000 111000110000	0000011011010100	798	000000000000 011100001000	0000101100101011
756	000000000000 111000011000	0000110111101011	799	000000000000 0111000001000	0001001000010000
757	000000000000 111000001100	0001100100111100	800	000000000000 0111000000100	0000100101010111
758	000000000000 1110000001100	0001101101000000	801	000000000000 0111000000010	0010001011000001
759	000000000000 1110000000110	0010101110010001	802	000000000000 0111000000001	0001001100010001
760	000000000000 1110000000011	0011000111010111	803	000000000000 0111000000000	0000001001001011
761	000000000000 1111000000000	0000001001001111	804	000000000000 0011111100000	0000100100101000
762	000000000000 1110100000000	0000010010010111	805	000000000000 0011101110000	0000100101101010
763	000000000000 1110010000000	0000100100100101	806	000000000000 0011100111000	0001101101101110
764	000000000000 1110001000000	0000001001011000	807	000000000000 0011100011100	0001010011111110
765	000000000000 1110000100000	0000010010001011	808	000000000000 0011100001110	0011110100010100
766	000000000000 1110000010000	0000100101100111	809	000000000000 0011100000111	0011110000010101
767	000000000000 1110000001000	0001000001011100	810	000000000000 0011110100000	0000101101110111
768	000000000000 1110000000100	0000101100011011	811	000000000000 0011101010000	0000110111100110
769	000000000000 1110000000010	0010000010001101	812	000000000000 0011100101000	0001001000001110
770	000000000000 1110000000001	0001000101011101	813	000000000000 0011100010100	0000010010100101
771	000000000000 1110000000000	0000000000000111	814	000000000000 0011100001010	0011011000001000
772	000000000000 0111111000000	0000110110100110	815	000000000000 0011100000101	0001110010011111
773	000000000000 0111011100000	0000110110111010	816	000000000000 0011111100000	0000110110100100
774	000000000000 0111001110000	0000110111111000	817	000000000000 0011101100000	0000000000001010
775	000000000000 0111000111000	0001111111111100	818	000000000000 0011100110000	0000101100110101
776	000000000000 0111000011100	0001000001101100	819	000000000000 0011100011000	0001111111100010
777	000000000000 0111000001110	0011100110000110	820	000000000000 0011100001100	0001110110011110
778	000000000000 0111000000111	0011100010000111	821	000000000000 0011100000110	0010110101001111

Sub-block 2

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
822	000000000000 001110000011	0011011100001001	869	000000000000 000011110000	0000101101100001
823	000000000000 001111000000	0000111111110111	870	000000000000 000011101000	0000011010001101
824	000000000000 001110100000	0000010010000110	871	000000000000 000011100100	0001111110110110
825	000000000000 001110010000	0000001001010101	872	000000000000 000011100010	0000010011110001
826	000000000000 001110001000	0000111110111001	873	000000000000 000011100001	0010111101100111
827	000000000000 001110000100	0001011010000010	874	000000000000 000011100000	0001111010110111
828	000000000000 001110000010	0000110111000101	875	000000000000 000011100000	0000111111101101
829	000000000000 001110000010	0010011001010011	876	000000000000 000001111110	0001110111010110
830	000000000000 001110000001	0001011110000011	877	000000000000 000001110110	0011010000111100
831	000000000000 001110000000	0000011011011001	878	000000000000 000001110011	0011010100111101
832	000000000000 000111111000	0000000001001001	879	000000000000 000001111010	0000110110001101
833	000000000000 000111011100	0001001001001101	880	000000000000 000001110101	0011111100100000
834	000000000000 000111001110	0001110111011101	881	000000000000 000001110010	0001010110110111
835	000000000000 000111000111	0011010000110111	882	000000000000 000001111100	0001011011001010
836	000000000000 000111000011	0011010100110110	883	000000000000 000001110110	0001010010110110
837	000000000000 000111101000	0000010011000101	884	000000000000 000001110011	0010010001100111
838	000000000000 000111010100	0001101100101101	885	000000000000 000001110001	0011111000100001
839	000000000000 000111001010	0000110110000110	886	000000000000 000001111000	0000011010010001
840	000000000000 000111000101	0011111100101011	887	000000000000 000001110100	0001111110101010
841	000000000000 000111000010	0001010110111100	888	000000000000 000001110010	0000010011101101
842	000000000000 000111111000	0000100100101001	889	000000000000 000001110001	0010111101111011
843	000000000000 000111011000	0000001000010110	890	000000000000 000001110000	0001111010101011
844	000000000000 000111001100	0001011011000001	891	000000000000 000001110000	0000111111110001
845	000000000000 000111000110	0001010010111101	892	000000000000 000000111110	0011010001111110
846	000000000000 000111000011	0010010001101100	893	000000000000 000000111011	0011010101111111
847	000000000000 000111000001	0011111000101010	894	000000000000 000000111101	0011111101100010
848	000000000000 000111100000	0000110110100101	895	000000000000 000000111010	0001010111110101
849	000000000000 000111010000	0000101101110110	896	000000000000 000000111110	0001010011110100
850	000000000000 000111001000	0000011010011010	897	000000000000 000000111010	0010010000100101
851	000000000000 000111000100	0001111110100001	898	000000000000 000000111001	0011111001100011
852	000000000000 000111000010	0000010011100110	899	000000000000 000000111100	0001111111010000
853	000000000000 000111000001	0010111101110000	900	000000000000 000000111010	0000010010101111
854	000000000000 000111000000	0001111010100000	901	000000000000 000000111001	0010111100111001
855	000000000000 000111000000	0000111111110101	902	000000000000 000000111000	0001111011101001
856	000000000000 000011111100	0001001001011010	903	000000000000 000000111000	0000111110110011
857	000000000000 000011101110	0001110111001010	904	000000000000 000000011111	0010011101111011
858	000000000000 000011100111	0011010000100000	905	000000000000 000000011101	0000011111110001
859	000000000000 000011100011	0011010100100001	906	000000000000 000000011110	0011011000100001
860	000000000000 000011110100	0001101100111010	907	000000000000 000000011101	0010110001100111
861	000000000000 000011101010	0000110110010001	908	000000000000 000000011110	0001011010101011
862	000000000000 000011100101	0011111100111100	909	000000000000 000000011101	0011110100111101
863	000000000000 000011100010	0001010110101011	910	000000000000 000000011100	0000110011101101
864	000000000000 000011111000	0000001000000001	911	000000000000 000000011100	0001110110110111
865	000000000000 000011101100	0001011011010110	912	000000000000 000000001111	0010001111110111
866	000000000000 000011100110	0001010010101010	913	000000000000 000000001101	0000001101111101
867	000000000000 000011100011	0010010001111011	914	000000000000 000000001110	0011001010101101
868	000000000000 000011100001	0011111000111101	915	000000000000 000000001100	0001001000100111

Sub-block 2

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
916	000000000000 000000001111	0010101010010111	963	000000000000 010101010000	000111111100100
917	000000000000 000000001110	0011101111001101	964	000000000000 010100101000	0000100101110101
918	000000000000 000000000111	0011101011001100	965	000000000000 010100010100	0001011010011101
919	000000000000 101111000000	0000111111111111	966	000000000000 010100001010	0000000000110110
920	000000000000 101011100000	0000111111101000	967	000000000000 0101000001010	0011001010011011
921	000000000000 101001110000	0000111111101010	968	000000000000 0101000000101	0001100000001100
922	000000000000 101000111000	0000111110110110	969	000000000000 010111000000	0000111111111000
923	000000000000 101000011100	0001110110110010	970	000000000000 010101100000	0000100100110111
924	000000000000 101000001110	0001001000100010	971	000000000000 010100110000	0000010010011001
925	000000000000 1010000001110	0011101111001000	972	000000000000 010100011000	0000111110100110
926	000000000000 1010000000111	0011101011001001	973	000000000000 010100001100	0001101101110001
927	000000000000 101101000000	0000101101101111	974	000000000000 0101000001100	0001100100001101
928	000000000000 101010100000	0000011011001010	975	000000000000 0101000000110	0010100111011100
929	000000000000 101001010000	0000110110101011	976	000000000000 0101000000011	0011001110011010
930	000000000000 101000101000	0000101100111010	977	000000000000 010110000000	0000011011011010
931	000000000000 101000010100	0001010011010010	978	000000000000 010101000000	0000101101101000
932	000000000000 101000001010	0000001001111001	979	000000000000 010100100000	0000000000010101
933	000000000000 1010000001010	0011000011010100	980	000000000000 010100010000	0000011011000110
934	000000000000 1010000000101	0001101001000011	981	000000000000 010100001000	0000101100101010
935	000000000000 101110000000	0000011011011101	982	000000000000 0101000001000	0001001000010001
936	000000000000 101011000000	0000110110110111	983	000000000000 0101000000100	0000100101010110
937	000000000000 101001100000	0000101101111000	984	000000000000 0101000000010	0010001011000000
938	000000000000 101000110000	0000011011010110	985	000000000000 0101000000001	0001001100010000
939	000000000000 101000011000	0000110111101001	986	000000000000 0101000000000	0000001001001010
940	000000000000 1010000011000	0001100100111110	987	000000000000 001011110000	0000101101100000
941	000000000000 1010000001100	0001101101000010	988	000000000000 001010111000	0000101100100010
942	000000000000 1010000000110	0010101110010011	989	000000000000 0010100111000	0001100100100110
943	000000000000 1010000000011	0011000111010101	990	000000000000 0010100011100	0001011010110110
944	000000000000 1011000000000	0000001001001101	991	000000000000 0010100001110	0011111101011100
945	000000000000 1010100000000	0000010010010101	992	000000000000 0010100000111	0011111001011101
946	000000000000 1010010000000	0000100100100111	993	000000000000 0010110100000	0000100100111111
947	000000000000 1010001000000	0000001001011010	994	000000000000 0010101010000	0000111110101110
948	000000000000 1010000100000	0000010010001001	995	000000000000 0010100101000	0001000001000110
949	000000000000 1010000010000	0000100101100101	996	000000000000 0010100010100	0000011011101101
950	000000000000 1010000001000	0001000001011110	997	000000000000 0010100001010	0011010001000000
951	000000000000 1010000000100	0000101100011001	998	000000000000 0010100000101	0001111011010111
952	000000000000 1010000000010	0010000010001111	999	000000000000 0010111000000	0000111111101100
953	000000000000 1010000000001	0001000101011111	1000	000000000000 0010101100000	0000001001000010
954	000000000000 1010000000000	0000000000000101	1001	000000000000 0010100110000	0000100101111101
955	000000000000 0101111000000	0000110110100111	1002	000000000000 0010100011000	0001110110101010
956	000000000000 0101011100000	0000110110111011	1003	000000000000 0010100001100	0001111111010110
957	000000000000 0101001110000	0000110111111001	1004	000000000000 0010100000110	0010111100000111
958	000000000000 0101000111000	0001111111111101	1005	000000000000 0010100000011	0011010101000001
959	000000000000 0101000011100	0001000001101101	1006	000000000000 0010110000000	0000110110110011
960	000000000000 0101000001110	0011100110000111	1007	000000000000 0010101000000	0000011011001110
961	000000000000 0101000000111	0011100010000110	1008	000000000000 0010100100000	0000000000011101
962	000000000000 0101101000000	0000010010000101	1009	000000000000 0010100010000	0000110111110001

Sub-block 2

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
1010	000000000000 0010100001000	0001010011001010	1057	000000000000 0000101000001	0001011110010101
1011	000000000000 0010100000100	0000111110001101	1058	000000000000 0000101000000	0000011011001111
1012	000000000000 0010100000010	0010010000011011	1059	000000000000 0000010111100	0001111110001001
1013	000000000000 0010100000001	0001010111001011	1060	000000000000 0000010101110	0011011001100011
1014	000000000000 0010100000000	0000010010010001	1061	000000000000 0000010100111	0011011101100010
1015	000000000000 0001011110000	0000010011011001	1062	000000000000 0000010110100	0000111111010010
1016	000000000000 0001010111000	0001011011011101	1063	000000000000 0000010101010	0011110101111111
1017	000000000000 0001010011100	0001100101001101	1064	000000000000 0000010100101	0001011111101000
1018	000000000000 0001010001110	0011000010100111	1065	000000000000 0000010111000	0001010010010101
1019	000000000000 0001010000111	0011000110100110	1066	000000000000 0000010101100	0001011011101001
1020	000000000000 0001011010000	0000000001010101	1067	000000000000 0000010100110	0010011000111000
1021	000000000000 0001010101000	0001111110111101	1068	000000000000 0000010100011	0011110001111110
1022	000000000000 0001010010100	0000100100010110	1069	000000000000 0000010110000	0000010011001110
1023	000000000000 0001010001010	0011101110111011	1070	000000000000 0000010101000	0001110111110101
1024	000000000000 0001010000101	0001000100101100	1071	000000000000 0000010100100	0000011010110010
1025	000000000000 0001011100000	0000110110111001	1072	000000000000 0000010100010	0010110100100100
1026	000000000000 0001010110000	0000011010000110	1073	000000000000 0000010100001	0001110011110100
1027	000000000000 0001010011000	0001001001010001	1074	000000000000 0000010100000	0000110110101110
1028	000000000000 0001010001100	0001000000101101	1075	000000000000 0000001011110	0011000011110010
1029	000000000000 0001010000110	0010000011111100	1076	000000000000 0000001010111	0011000111110011
1030	000000000000 0001010000011	0011101010111010	1077	000000000000 0000001011010	0011101111101110
1031	000000000000 0001011000000	0000100100110101	1078	000000000000 0000001010101	0001000101111001
1032	000000000000 0001010100000	0000111111100110	1079	000000000000 0000001011100	0001000001111000
1033	000000000000 0001010010000	0000001000001010	1080	000000000000 0000001010110	0010000010101001
1034	000000000000 0001010001000	0001101100110001	1081	000000000000 0000001010011	0011101011101111
1035	000000000000 0001010000100	0000000001110110	1082	000000000000 0000001011000	0001101101100100
1036	000000000000 0001010000010	0010101111100000	1083	000000000000 0000001010100	0000000000100011
1037	000000000000 0001010000001	0001101000110000	1084	000000000000 0000001010010	0010101110110101
1038	000000000000 0001010000000	0000101101101010	1085	000000000000 0000001010001	0001101001100101
1039	000000000000 0000101111000	0001101101111000	1086	000000000000 0000001010000	0000101100111111
1040	000000000000 0000101011100	0001010011101000	1087	000000000000 0000000101111	0010111000011011
1041	000000000000 0000101001110	0011110100000010	1088	000000000000 0000000101101	0000111010010001
1042	000000000000 0000101000111	0011110000000011	1089	000000000000 0000000101110	0011111101000001
1043	000000000000 0000101101000	0001001000011000	1090	000000000000 0000000101011	0010010100000111
1044	000000000000 0000101010100	0000010010110011	1091	000000000000 0000000101100	0001111111001011
1045	000000000000 0000101001010	0011011000011110	1092	000000000000 0000000101010	0011010001011101
1046	000000000000 0000101000101	0001110010001001	1093	000000000000 0000000101001	0000010110001101
1047	000000000000 0000101110000	0000101100100011	1094	000000000000 0000000101000	0001010011010111
1048	000000000000 0000101011000	0001111111110100	1095	000000000000 0000000010111	0011001110101100
1049	000000000000 0000101001100	0001110110001000	1096	000000000000 0000000010101	0001001100100110
1050	000000000000 0000101000110	0010110101011001	1097	000000000000 0000000010110	0010001011110110
1051	000000000000 0000101000011	0011011100011111	1098	000000000000 0000000010100	0000001001111100
1052	000000000000 0000101100000	0000001001000011	1099	000000000000 0000000001011	0010000110001011
1053	000000000000 0000101010000	0000111110101111	1100	000000000000 0000000001010	0011000011010001
1054	000000000000 0000101001000	0001011010010100	1101	000000000000 0000000000101	0001101001000110
1055	000000000000 0000101000100	0000110111010011	1102	000000000000 1101110000000	0000111111111100
1056	000000000000 0000101000010	0010011001000101	1103	000000000000 1100111000000	0000111111101011

Sub-block 2

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
1104	000000000000 110001110000	000011111110111	1151	000000000000 011000000101	0001101001000101
1105	000000000000 110000111000	000011110110101	1152	000000000000 011011000000	0000110110110001
1106	000000000000 110000011100	0001110110110001	1153	000000000000 011001100000	0000101101111110
1107	000000000000 110000001110	0001001000100001	1154	000000000000 011000110000	0000011011010000
1108	000000000000 110000000111	0011101111001011	1155	000000000000 011000011000	0000110111101111
1109	000000000000 110000000011	0011101011001010	1156	000000000000 011000001100	0001100100111000
1110	000000000000 110101000000	0000101101101100	1157	000000000000 011000000110	0001101101000100
1111	000000000000 110010100000	0000011011001001	1158	000000000000 011000000011	0010101110010101
1112	000000000000 110001010000	0000110110101000	1159	000000000000 011000000001	0011000111010011
1113	000000000000 110000101000	0000101100111001	1160	000000000000 011010000000	0000010010010011
1114	000000000000 110000010100	0001010011010001	1161	000000000000 011001000000	0000100100100001
1115	000000000000 110000001010	0000001001111010	1162	000000000000 011000100000	0000001001011100
1116	000000000000 110000000101	0011000011010111	1163	000000000000 011000010000	0000010010001111
1117	000000000000 110000000010	0001101001000000	1164	000000000000 011000001000	0000100101100011
1118	000000000000 110110000000	0000011011011110	1165	000000000000 011000000100	0001000001011000
1119	000000000000 110011000000	0000110110110100	1166	000000000000 011000000010	0000101100011111
1120	000000000000 110001100000	0000101101111011	1167	000000000000 011000000001	0010000010001001
1121	000000000000 110000110000	0000011011010101	1168	000000000000 011000000000	0001000101011001
1122	000000000000 110000011000	0000110111101010	1169	000000000000 001101110000	0000000000000011
1123	000000000000 110000001100	0001100100111101	1170	000000000000 001100111000	0000110110111000
1124	000000000000 110000000110	0001101101000001	1171	000000000000 001100111000	0000110111111010
1125	000000000000 110000000011	0010101110010000	1172	000000000000 001100011100	0001111111111110
1126	000000000000 110000000001	0011000111010110	1173	000000000000 001100001110	0001000001101110
1127	000000000000 110100000000	0000001001001110	1174	000000000000 001100000110	0011100110000100
1128	000000000000 110010000000	0000010010010110	1175	000000000000 001100000011	0011100010000101
1129	000000000000 110001000000	0000100100100100	1176	000000000000 001101010000	0000111111100111
1130	000000000000 110000100000	0000001001011001	1177	000000000000 001100101000	0000100101110110
1131	000000000000 110000010000	0000010010001010	1178	000000000000 001100010100	0001011010011110
1132	000000000000 110000001000	0000100101100110	1179	000000000000 001100001010	0000000000110101
1133	000000000000 110000000100	0001000001011101	1180	000000000000 001100000101	0011001010011000
1134	000000000000 110000000010	0000101100011010	1181	000000000000 001100000010	0001100000001111
1135	000000000000 110000000001	0010000010001100	1182	000000000000 001101100000	0000100100110100
1136	000000000000 110000000000	0001000101011100	1183	000000000000 001100110000	0000010010011010
1137	000000000000 110000000000	0000000000000110	1184	000000000000 001100011000	0000111110100101
1138	000000000000 011011100000	0000111111101110	1185	000000000000 001100001100	0001101101110010
1139	000000000000 011001110000	000011111110010	1186	000000000000 001100000110	0001100100001110
1140	000000000000 011000111000	000011110110000	1187	000000000000 001100000011	0010100111011111
1141	000000000000 011000011100	0001110110110100	1188	000000000000 001100000001	0011001110011001
1142	000000000000 011000001110	0001001000100100	1189	000000000000 001101000000	0000101101101011
1143	000000000000 011000000111	0011101111001110	1190	000000000000 001100100000	0000000000010110
1144	000000000000 011000000011	0011101011001111	1191	000000000000 001100010000	0000011011000101
1145	000000000000 011010100000	0000011011001100	1192	000000000000 001100001000	0000101100101001
1146	000000000000 011001010000	0000110110101101	1193	000000000000 001100000100	0001001000010010
1147	000000000000 011000101000	0000101100111100	1194	000000000000 001100000010	0000100101010101
1148	000000000000 011000010100	0001010011010100	1195	000000000000 001100000001	0010001011000011
1149	000000000000 011000001010	0000001001111111	1196	000000000000 001100000000	0001001100010011
1150	000000000000 011000000101	0011000011010010	1197	000000000000 001100000000	0000001001001001

Sub-block 2

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
1198	000000000000 0001101110000	0000100101101011	1245	000000000000 0000011010100	0000100100000001
1199	000000000000 0001100111000	0001101101101111	1246	000000000000 0000011001010	0011101110101100
1200	000000000000 0001100011100	0001010011111111	1247	000000000000 0000011000101	0001000100111011
1201	000000000000 0001100001110	0011110100010101	1248	000000000000 0000011011000	0001001001000110
1202	000000000000 0001100000111	0011110000010100	1249	000000000000 0000011001100	0001000000111010
1203	000000000000 0001101010000	0000110111100111	1250	000000000000 0000011000110	0010000011101011
1204	000000000000 0001100101000	0001001000001111	1251	000000000000 0000011000011	0011101010101101
1205	000000000000 0001100010100	0000010010100100	1252	000000000000 0000011010000	0000001000011101
1206	000000000000 0001100001010	0011011000001001	1253	000000000000 0000011001000	0001101100100110
1207	000000000000 0001100000101	0001110010011110	1254	000000000000 0000011000100	0000000001100001
1208	000000000000 0001101100000	0000000000001011	1255	000000000000 0000011000010	0010101111110111
1209	000000000000 0001100110000	0000101100110100	1256	000000000000 0000011000001	0001101000100111
1210	000000000000 0001100011000	0001111111100011	1257	000000000000 0000011000000	0000101101111101
1211	000000000000 0001100001100	0001110110011111	1258	000000000000 0000001101110	0011110100011110
1212	000000000000 0001100000110	0010110101001110	1259	000000000000 0000001100111	0011110000011111
1213	000000000000 0001100000011	0011011100001000	1260	000000000000 0000001101010	0011011000000010
1214	000000000000 0001101000000	0000010010000111	1261	000000000000 0000001100101	0001110010010101
1215	000000000000 0001100100000	0000001001010100	1262	000000000000 0000001101100	0001110110010100
1216	000000000000 0001100010000	0000111110111000	1263	000000000000 0000001100110	0010110101000101
1217	000000000000 0001100001000	0001011010000011	1264	000000000000 0000001100011	0011011100000011
1218	000000000000 0001100000100	0000110111000100	1265	000000000000 0000001101000	0001011010001000
1219	000000000000 0001100000010	0010011001010010	1266	000000000000 0000001100100	0000110111001111
1220	000000000000 0001100000001	0001011110000010	1267	000000000000 0000001100010	0010011001011001
1221	000000000000 0001100000000	0000011011011000	1268	000000000000 0000001100001	0001011110001001
1222	000000000000 0000110111000	0001000000000101	1269	000000000000 0000001100000	0000011011010011
1223	000000000000 0000110011100	0001111110010101	1270	000000000000 0000000110111	0011011100100000
1224	000000000000 0000110001110	0011011001111111	1271	000000000000 0000000110101	0001011110101010
1225	000000000000 0000110000111	0011011101111110	1272	000000000000 0000000110110	0010011001111010
1226	000000000000 0000110101000	0001100101100101	1273	000000000000 0000000110011	0011110000111100
1227	000000000000 0000110010100	0000111111001110	1274	000000000000 0000000110100	0000011011110000
1228	000000000000 0000110001010	0011110101100011	1275	000000000000 0000000110010	0010110101100110
1229	000000000000 0000110000101	0001011111110100	1276	000000000000 0000000110001	0001110010110110
1230	000000000000 0000110110000	0000000001011110	1277	000000000000 0000000110000	0000110111101100
1231	000000000000 0000110011000	0001010010001001	1278	000000000000 0000000011011	0010100011101011
1232	000000000000 0000110001100	0001011011110101	1279	000000000000 0000000011001	0000100001100001
1233	000000000000 0000110000110	0010011000100100	1280	000000000000 0000000011010	0011100110110001
1234	000000000000 0000110000011	0011110001100010	1281	000000000000 0000000011000	0001100100111011
1235	000000000000 0000110100000	0000100100111110	1282	000000000000 0000000001101	0000101000011101
1236	000000000000 0000110010000	0000010011010010	1283	000000000000 0000000001100	0001101101000111
1237	000000000000 0000110001000	0001110111101001	1284	000000000000 0000000000110	0010101110010110
1238	000000000000 0000110000100	0000011010101110	1285	000000000000 0000000000011	0011000111010000
1239	000000000000 0000110000010	0010110100111000	1286	000000000000 1001110000000	0000111111111110
1240	000000000000 0000110000001	0001110011101000	1287	000000000000 1000111000000	0000111111101001
1241	000000000000 0000110000000	0000110110110010	1288	000000000000 1000011100000	0000111111101010
1242	000000000000 0000011011100	0001100101011010	1289	000000000000 1000001110000	0000111101101111
1243	000000000000 0000011001110	0011000010110000	1290	000000000000 1000000111000	0001110110110011
1244	000000000000 0000011000111	0011000110110001	1291	000000000000 1000000011100	0001001000100011

Sub-block 2

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
1292	000000000000 100000001110	0011101111001001	1339	000000000000 010000110000	000110111101110
1293	000000000000 100000000111	0011101011001000	1340	000000000000 010000011000	0001100100111001
1294	000000000000 100101000000	0000101101101110	1341	000000000000 010000001100	0001101101000101
1295	000000000000 100010100000	0000011011001011	1342	000000000000 010000000110	0010101110010100
1296	000000000000 100001010000	0000110110101010	1343	000000000000 010000000011	0011000111010010
1297	000000000000 100000101000	0000101100111011	1344	000000000000 010010000000	0000010010010010
1298	000000000000 100000010100	0001010011010011	1345	000000000000 010001000000	0000100100100000
1299	000000000000 100000001010	0000001001111000	1346	000000000000 010000100000	0000001001011101
1300	000000000000 1000000001010	0011000011010101	1347	000000000000 010000010000	0000010010001110
1301	000000000000 1000000000101	0001101001000010	1348	000000000000 010000001000	0000100101100010
1302	000000000000 100110000000	0000011011011100	1349	000000000000 0100000001000	0001000001011001
1303	000000000000 100011000000	0000110110110110	1350	000000000000 0100000000100	0000101100011110
1304	000000000000 100001100000	0000101101111001	1351	000000000000 0100000000010	0010000010001000
1305	000000000000 100000110000	0000011011010111	1352	000000000000 0100000000001	0001000101011000
1306	000000000000 100000011000	0000110111101000	1353	000000000000 0100000000000	0000000000000010
1307	000000000000 1000000011000	0001100100111111	1354	000000000000 0010011100000	0000111111110000
1308	000000000000 1000000001100	0001101101000011	1355	000000000000 0010001110000	0000111110110010
1309	000000000000 1000000000110	0010101110010010	1356	000000000000 0010000111000	0001110110110110
1310	000000000000 1000000000011	0011000111010100	1357	000000000000 0010000011100	0001001000100110
1311	000000000000 1001000000000	0000001001001100	1358	000000000000 0010000001110	0011101111001100
1312	000000000000 1000100000000	0000010010010100	1359	000000000000 0010000000111	0011101011001101
1313	000000000000 1000010000000	0000100100100110	1360	000000000000 0010010100000	0000110110101111
1314	000000000000 1000001000000	0000001001011011	1361	000000000000 0010001010000	0000101100111110
1315	000000000000 1000000100000	0000010010001000	1362	000000000000 0010000101000	0001010011010110
1316	000000000000 1000000010000	0000100101100100	1363	000000000000 0010000010100	0000001001111101
1317	000000000000 1000000001000	0001000001011111	1364	000000000000 0010000001010	0011000011010000
1318	000000000000 1000000000100	0000101100011000	1365	000000000000 0010000000101	0001101001000111
1319	000000000000 1000000000010	0010000010001110	1366	000000000000 0010011000000	0000101101111100
1320	000000000000 1000000000001	0001000101011110	1367	000000000000 0010001100000	0000011011010010
1321	000000000000 1000000000000	0000000000000100	1368	000000000000 0010000110000	0000110111101101
1322	000000000000 0100111000000	0000111111101111	1369	000000000000 0010000011000	0001100100111010
1323	000000000000 0100011100000	0000111111110011	1370	000000000000 0010000001100	0001101101000110
1324	000000000000 0100001110000	0000111110110001	1371	000000000000 0010000000110	0010101110010111
1325	000000000000 0100000111000	0001110110110101	1372	000000000000 0010000000011	0011000111010001
1326	000000000000 0100000011100	0001001000100101	1373	000000000000 0010010000000	0000100100100011
1327	000000000000 0100000001110	0011101111001111	1374	000000000000 0010001000000	0000001001011110
1328	000000000000 0100000000111	0011101011001110	1375	000000000000 0010000100000	0000010010001101
1329	000000000000 0100101000000	0000011011001101	1376	000000000000 0010000010000	0000100101100001
1330	000000000000 0100010100000	0000110110101100	1377	000000000000 0010000001000	0001000001011010
1331	000000000000 0100001010000	0000101100111101	1378	000000000000 0010000000100	0000101100011101
1332	000000000000 0100000101000	0001010011010101	1379	000000000000 0010000000010	0010000010001011
1333	000000000000 0100000010100	0000001001111110	1380	000000000000 0010000000001	0001000101011011
1334	000000000000 0100000001010	0011000011010011	1381	000000000000 0010000000000	0000000000000001
1335	000000000000 0100000000101	0001101001000100	1382	000000000000 0001001110000	0000101111111011
1336	000000000000 0100110000000	0000110110110000	1383	000000000000 0001000111000	0001111111111111
1337	000000000000 0100011000000	0000101101111111	1384	000000000000 0001000011100	0001000001101111
1338	000000000000 0100001100000	0000011011010001	1385	000000000000 0001000001110	0011100110000101

Sub-block 2

S.No.	Error Vector	Syndrome	S. no.	Error vector	Syndrome
1386	000000000000 000100000111	0011100010000100	1429	000000000000 0000010010100	0000101101011110
1387	000000000000 0001001010000	0000100101110111	1430	000000000000 0000010001010	0011100111110011
1388	000000000000 0001000101000	0001011010011111	1431	000000000000 0000010000101	0001001101100100
1389	000000000000 0001000010100	0000000000110100	1432	000000000000 0000010011000	0001000000011001
1390	000000000000 0001000001010	0011001010011001	1433	000000000000 0000010001100	0001001001100101
1391	000000000000 0001000000101	0001100000001110	1434	000000000000 0000010000110	0010001010110100
1392	000000000000 0001001100000	0000010010011011	1435	000000000000 0000010000011	0011100011110010
1393	000000000000 0001000110000	0000111110100100	1436	000000000000 0000010010000	0000000001000010
1394	000000000000 0001000011000	0001101101110011	1437	000000000000 0000010001000	0001100101111001
1395	000000000000 0001000001100	0001100100001111	1438	000000000000 0000010000100	0000001000111110
1396	000000000000 0001000000110	0010100111011110	1439	000000000000 0000010000010	0010100110101000
1397	000000000000 0001000000011	0011001110011000	1440	000000000000 0000010000001	0001100001111000
1398	000000000000 0001001000000	0000000000010111	1441	000000000000 0000010000000	0000100100100010
1399	000000000000 0001000100000	0000011011000100	1442	000000000000 0000001001110	0011100110010010
1400	000000000000 0001000010000	0000101100101000	1443	000000000000 0000001000111	0011100010010011
1401	000000000000 0001000001000	0001001000010011	1444	000000000000 0000001001010	0011001010001110
1402	000000000000 0001000000100	0000100101010100	1445	000000000000 0000001000101	0001100000011001
1403	000000000000 0001000000010	0010001011000010	1446	000000000000 0000001001100	0001100100011000
1404	000000000000 0001000000001	0001001100010010	1447	000000000000 0000001000110	0010100111001001
1405	000000000000 0001000000000	0000001001001000	1448	000000000000 0000001000011	0011001110001111
1406	000000000000 0000100111000	0001100100100111	1449	000000000000 0000001001000	0001001000000100
1407	000000000000 0000100011100	0001011010101011	1450	000000000000 0000001000100	0000100101000011
1408	000000000000 0000100001110	0011111101011101	1451	000000000000 0000001000010	0010001011010101
1409	000000000000 0000100000111	0011111001011100	1452	000000000000 0000001000001	0001001100000101
1410	000000000000 0000100101000	0001000001000111	1453	000000000000 0000001000000	0000001001011111
1411	000000000000 0000100010100	0000011011101100	1454	000000000000 0000000100111	0011111001000000
1412	000000000000 0000100001010	0011010001000001	1455	000000000000 0000000100101	0001111011001010
1413	000000000000 0000100000101	0001111011010110	1456	000000000000 0000000100110	0010111100011010
1414	000000000000 0000100110000	0000100101111100	1457	000000000000 0000000100011	0011010101011100
1415	000000000000 0000100011000	0001110110101011	1458	000000000000 0000000100100	0000111110010000
1416	000000000000 0000100001100	0001111111010111	1459	000000000000 0000000100010	0010010000000110
1417	000000000000 0000100000110	0010111100000110	1460	000000000000 0000000100001	0001010111010110
1418	000000000000 0000100000011	0011010101000000	1461	000000000000 0000000100000	0000010010001100
1419	000000000000 0000100100000	0000000000011100	1462	000000000000 0000000010011	0011100010110000
1420	000000000000 0000100010000	0000110111110000	1463	000000000000 0000000010001	0001100000111010
1421	000000000000 0000100001000	0001010011001011	1464	000000000000 0000000010010	0010100111101010
1422	000000000000 0000100000100	0000111110001100	1465	000000000000 0000000010000	0000100101100000
1423	000000000000 0000100000010	0010010000011010	1466	000000000000 0000000001001	0000000100000001
1424	000000000000 0000100000001	0001010111001010	1467	000000000000 0000000001000	0001000001011011
1425	000000000000 0000100000000	0000010010010000	1468	000000000000 0000000000100	0000101100011100
1426	000000000000 0000010011100	0001101100000101	1469	000000000000 0000000000010	0010000010001010
1427	000000000000 0000010001110	0011001011101111	1470	000000000000 0000000000001	0001000101011010
1428	000000000000 0000010000111	0011001111101110			

III Bounds for codes correcting m -repeated bursts

In this section, we extend the results of previous section to the case of m -repeated bursts of length b or less occurring within a single sub-block.

Similar to the case of correction of 2-repeated burst occurring within a sub-block, an (n, k) linear code over $GF(q)$ capable of correcting any sub-block containing m -repeated burst of length b or less must satisfy the following two conditions:

- (v) The syndrome resulting from the occurrence of any m -repeated burst of length b or less within a single sub-block must be distinct from the syndrome resulting from any other m -repeated burst within the same sub-block.
- (vi) The syndrome resulting from the occurrence of any m -repeated burst of length b or less within a single sub-block must be distinct from the syndrome resulting likewise from any m -repeated burst of length b or less within any other sub-block.

We now present a lower bound on the number of parity check digits required for such a code.

Theorem 3. *The number of check digits r required for an (n, k) linear code over $GF(q)$, subdivided into s sub-blocks of length t each, that corrects m -repeated bursts of length b or less lying within a single corrupted sub-block is atleast*

$$\log_q \left\{ 1 + s \left[q^{m(b-1)} \binom{t - mb + m}{m} (q - 1)^m + \sum_{l=0}^{m-1} \binom{t - mb + l}{l} (q - 1)^l q^{m-1-l} - 1 \right] \right\}. \quad (9)$$

Proof. The proof of this result is on the similar lines as that of proof of Theorem 1 so we omit the proof.

□

Remark 4. By taking $s = 1$ the bound obtained in (9) reduces to

$$\log_q \left\{ q^{m(b-1)} \left(\binom{t - mb + m}{m} (q - 1)^m + \sum_{l=0}^{m-1} \binom{t - mb + l}{l} (q - 1)^l q^{m-1-l} \right) \right\}.$$

which coincides with the result for correction of m -repeated burst obtained by Dass and Verma(2008).

Remark 5. For $m = 2$, the bound obtained in (9) coincides with the bound obtained in (1) for the case of 2-repeated bursts.

In particular, for $m = 1$, the bound in (9) reduces to

$$1 + s \left(q^{b-1} ((t - b + 1)(q - 1) + 1) - 1 \right)$$

which reduces to the result for correction of burst of length b or less within a sub-block.

In the following result, we present another bound on the number of check digits required for the existence of the code considered in Theorem 3.

Theorem 4. *An (n, k) linear code over $GF(q)$ capable of correcting m -repeated burst of length b or less occurring within a single sub-block of length t ($2mb < t$) can always be constructed using r check digits where r is the smallest integer satisfying the inequality*

$$q^r > q^{m(b-1)} \left\{ q^{m(b-1)} \binom{t - 2mb + (2m - 1)}{2m - 1} + \sum_{l=0}^{2m-2} (q - 1)^l q^{2m-2-l} \binom{t - 2mb + l}{l} + \left((s - 1) \times \left[(q - 1)^{m-1} \binom{t - mb + (m - 1)}{m - 1} + \sum_{l=0}^{m-2} (q - 1)^l q^{m-2-l} \binom{t - mb + l}{l} \right] \times \left[q^{m(b-1)} \binom{t - mb + m}{m} (q - 1)^m + \sum_{l=0}^{m-1} \binom{t - mb + l}{l} (q - 1)^l q^{m-1-l} - 1 \right] \right) \right\}. \tag{10}$$

Proof. As in Theorem 3, we omit the proof of this result since it can be derived on lines similar to that of Theorem 2.

□

Remark 6. By taking $s = 1$ in (10) the bound reduces to

$$q^r > q^{2m(b-1)} \left((q-1)^{2m-1} \binom{t-2mb+(2m-1)}{2m-1} + \sum_{l=0}^{2m-2} (q-1)^l q^{2m-2-l} \binom{t-2mb+l}{l} \right)$$

which coincides with the sufficient condition for existence of a code correcting m -repeated bursts(refer Dass and Verma(2008)).

Remark 7. For $m = 2$, the result obtained in Theorem 4 coincides with the result in Theorem 2, for the case of 2-repeated burst of length b or less.

For $m = 1$, the bound in (10) reduces to

$$q^{b-1} \left(q^{b-1} \left[(q-1)(t-2b+1) + 1 \right] + (s-1) \left[q^{b-1} \left((t-b+1)(q-1) + 1 \right) - 1 \right] \right)$$

which is the condition for existence of a code correcting bursts of length b or less within a sub-block.

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